

Prime Number Theorem



Professor
Jaehyun Cho (UNIST)

May 12, 2022 16:00 - 17:15

>>> Venue (110-N103) <<<

Host

Professor
Chol Park

E-mail
cholpark@unist.ac.kr

Abstract

This lecture is targeting a general math students. We show that there are infinitely many prime numbers in two ways. After that, we explore the distribution of prime numbers. Let $\pi(x)$ be the number of primes less than or equal to x . Before we prove the famous PNT (prime number theorem), we show that for $x \geq 2$,

$$\left(\frac{3 \log 2}{8}\right) \frac{x}{\log x} < \pi(x) < (6 \log 2) \frac{x}{\log x}.$$

Note that $3 \log / 8 = 0.259940\dots$, $6 \log 2 = 4.15888\dots$

Lastly, we prove the PNT.

Theorem (PNT) AS $x \rightarrow \infty$

$$\pi(x) \sim \frac{x}{\log x}.$$